Algebra 1

An Incremental Development

Third Edition

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Contents

	Preface	xi
Lesson 1	Addition and Subtraction of Fractions • Lines and Segments	1
Lesson 2	Angles • Polygons • Triangles • Quadrilaterals	4
Lesson 3	Perimeter • Circumference	10
Lesson 4	Review of Arithmetic	14
Lesson 5	Sets • Absolute Value • Addition of Signed Numbers	23
Lesson 6	Rules for Addition • Adding More Than Two Numbers • Inserting Parentheses Mentally • Definition of Subtraction	29
Lesson 7	The Opposite of a Number • Simplifying More Difficult Notations	34
Lesson 8	Area	36
Lesson 9	Rules for Multiplication of Signed Numbers • Inverse Operations • Rules for Division of Signed Numbers • Summary	43
Lesson 10	Division by Zero • Exchange of Factors in Multiplication • Conversions of Area	47
Lesson 11	Reciprocal and Multiplicative Inverse • Order of Operations • Identifying Multiplication and Addition	51
Lesson 12	Symbols of Inclusion • Order of Operations	54
Lesson 13	Multiple Symbols of Inclusion • More on Order of Operations • Products of Signed Numbers	57
Lesson 14	Evaluation of Algebraic Expressions	63
Lesson 15	Surface Area	67
Lesson 16	More Complicated Evaluations	72
Lesson 17	Factors and Coefficients • Terms • The Distributive Property	74
Lesson 18	Like Terms • Addition of Like Terms	79
esson 19	Exponents • Powers of Negative Numbers • Roots • Evaluation of Powers	82
esson 20	Volume	86

vi Contents

Lesson 21	Product Rule for Exponents • Addition of Like Terms with Exponents	91
Lesson 22	Review of Numerical and Algebraic Expressions • Statements and Sentences • Conditional Equations	95
Lesson 23	Equivalent Equations • Additive Property of Equality	99
Lesson 24	Multiplicative Property of Equality	102
Lesson 25	Solution of Equations	106
Lesson 26	More Complicated Equations	110
Lesson 27	More on the Distributive Property • Simplifying Decimal Equations	113
Lesson 28	Fractional Parts of Numbers • Functional Notation	116
Lesson 29	Negative Exponents • Zero Exponents	121
Lesson 30	Algebraic Phrases • Decimal Parts of a Number	125
Lesson 31	Equations with Parentheses	128
Lesson 32	Word Problems	131
Lesson 33	Products of Prime Factors • Statements About Unequal Quantities	134
Lesson 34	Greatest Common Factor	138
Lesson 35	Factoring the Greatest Common Factor • Canceling	140
Lesson 36	Distributive Property of Rational Expressions that Contain Positive Exponents • Minus Signs and Negative Exponents	146
Lesson 37	Inequalities • Greater Than and Less Than • Graphical Solutions of Inequalities	149
Lesson 38	Ratio Problems	153
Lesson 39	Trichotomy Axiom • Negated Inequalities • Advanced Ratio Problems	156
Lesson 40	Quotient Rule for Exponents • Distributive Property of Rational Expressions that Contain Negative Exponents	160
Lesson 41	Addition of Like Terms in Rational Expressions • Two-Step Problems	165
Lesson 42	Solving Multivariable Equations	168
Lesson 43	Least Common Multiple • Least Common Multiples of Algebraic Expressions	171
Lesson 44	Addition of Rational Expressions with Equal Denominators • Addition of Rational Expressions with Unequal Denominators	176
Lesson 45	Range, Median, Mode, and Mean	181
Lesson 46	Conjunctions	185
Lesson 47	Percents Less Than 100 • Percents Greater Than 100	187
Lesson 48	Polynomials • Degree • Addition of Polynomials	192
Lesson 49	Multiplication of Polynomials	197
Lesson 50	Polynomial Equations • Ordered Pairs • Cartesian Coordinate System	200

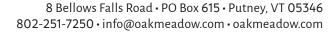
VII Contents

Lesson 51	Graphs of Linear Equations • Graphs of Vertical and Horizontal Lines	205
Lesson 52	More on Addition of Rational Expressions with Unequal Denominators • Overall Average	211
Lesson 53	Power Rule for Exponents • Conversions of Volume	215
Lesson 54	Substitution Axiom • Simultaneous Equations • Solving Simultaneous Equations by Substitution	218
Lesson 55	Complex Fractions • Division Rule for Complex Fractions	224
Lesson 56	Finite and Infinite Sets • Membership in a Set • Rearranging Before Graphing	228
Lesson 57	Addition of Algebraic Expressions with Negative Exponents	232
Lesson 58	Percent Word Problems	235
Lesson 59	Rearranging Before Substitution	239
Lesson 60	Geometric Solids • Prisms and Cylinders	242
Lesson 61	Subsets • Subsets of the Set of Real Numbers	247
Lesson 62	Square Roots • Higher Order Roots • Evaluating Using Plus or Minus	252
Lesson 63	Product of Square Roots Rule • Repeating Decimals	257
Lesson 64	Domain • Additive Property of Inequality	260
Lesson 65	Addition of Radical Expressions • Weighted Average	264
Lesson 66	Simplification of Radical Expressions • Square Roots of Large Numbers	268
Lesson 67	Review of Equivalent Equations • Elimination	271
Lesson 68	More About Complex Fractions	276
Lesson 69	Factoring Trinomials	280
Lesson 70	Probability • Designated Order	284
Lesson 71	Trinomials with Common Factors • Subscripted Variables	288
Lesson 72	Factors That Are Sums • Pyramids and Cones	292
Lesson 73	Factoring the Difference of Two Squares • Probability Without Replacement	298
Lesson 74	Scientific Notation	301
Lesson 75	Writing the Equation of a Line • Slope-Intercept Method of Graphing	305
Lesson 76	Consecutive Integers	313
Lesson 77	Consecutive Odd and Consecutive Even Integers • Fraction and Decimal Word Problems	316
Lesson 78	Rational Equations	320
Lesson 79	Systems of Equations with Subscripted Variables	323
Lesson 80	Operations with Scientific Notation	326

viii Contents

Lesson 81	Graphical Solutions • Inconsistent Equations • Dependent Equations	330
Lesson 82	Evaluating Functions • Domain and Range	337
Lesson 83	Coin Problems	342
Lesson 84	Multiplication of Radicals • Functions	345
Lesson 85	Stem-and-Leaf Plots • Histograms	351
Lesson 86	Division of Polynomials	357
Lesson 87	More on Systems of Equations • Tests for Functions	362
Lesson 88	Quadratic Equations • Solution of Quadratic Equations by Factoring	367
Lesson 89	Value Problems	371
Lesson 90	Word Problems with Two Statements of Equality	374
Lesson 91	Multiplicative Property of Inequality • Spheres	378
Lesson 92	Uniform Motion Problems About Equal Distances	383
Lesson 93	Products of Rational Expressions • Quotients of Rational Expressions	388
Lesson 94	Uniform Motion Problems of the Form $D_1 + D_2 = N$	391
Lesson 95	Graphs of Non-Linear Functions • Recognizing Shapes of Various Non-Linear Functions	395
Lesson 96	Difference of Two Squares Theorem	402
Lesson 97	Angles and Triangles • Pythagorean Theorem • Pythagorean Triples	405
Lesson 98	Distance Between Two Points • Slope Formula	412
Lesson 99	Uniform Motion—Unequal Distances	418
Lesson 100	Place Value • Rounding Numbers	422
Lesson 101	Factorable Denominators	427
Lesson 102	Absolute Value Inequalities	430
Lesson 103	More on Rational Equations	435
Lesson 104	Abstract Rational Equations	439
Lesson 105	Factoring by Grouping	443
Lesson 106	Linear Equations • Equation of a Line Through Two Points	446
Lesson 107	Line Parallel to a Given Line • Equation of a Line with a Given Slope	450
Lesson 108	Square Roots Revisited • Radical Equations	454
Lesson 109	Advanced Trinomial Factoring	458
Lesson 110	Vertical Shifts • Horizontal Shifts • Reflection About the <i>x</i> Axis • Combinations of Shifts and Reflections	462
Lesson 111	More on Conjunctions • Disjunctions	468
Lesson 112	More on Multiplication of Radical Expressions	471
Lesson 113	Direct Variation • Inverse Variation	473

	ix	Contents
Lesson 114	Exponential Key • Exponential Growth • Using the Graphing Calculator to Graph Exponential Functions	479
Lesson 115	Linear Inequalities	485
Lesson 116	Quotient Rule for Square Roots	490
Lesson 117	Direct and Inverse Variation Squared	493
Lesson 118	Completing the Square	496
Lesson 119	The Quadratic Formula • Use of the Quadratic Formula	501
Lesson 120	Box-and-Whisker Plots	505
Appendix A	Properties of the Set of Real Numbers	511
Appendix B	Glossary	515
	Answers	523
	Index	557





Algebra I Syllabus

Textbook

Algebra I: An Incremental Development (Saxon)

Materials

Algebra I textbook

Homeschool Packet: Practice tests (formerly called Form A tests), answers to problem sets and practice tests

Schedule of Assignments

As an independent study student, you can complete this course at your own pace. Some students benefit from doing every single problem in the problem sets while others prefer to do all the even numbered problems, and then go back and do the odd numbered problems for skills that need extra practice. By checking your answers after each problem set, you can gauge how well you are grasping the material and adjust your work load accordingly.

There is a proposed schedule of assignments on the back that will help you move through the course in 30 weeks. Feel free to adjust this schedule to suit your needs and learning style.

We wish you a challenging and successful year of Algebra !!

Algebra I Assignment Sheet

Lesson	Problem Sets	Tests
1	1–4	1
2	5–8	2
3	9–12	3
4	13–16	4
5	17–20	5
6	21–24	6
7	25–28	7
8	29–32	8
9	33–36	9
10	37–40	10
11	41–44	11
12	45–48	12
13	49–52	13
14	53–56	14
15	57–60	15
16	61–64	16
17	65–68	17
18	69–72	18
19	73–76	19
20	77–80	20
21	81–84	21
22	85–88	22
23	89–92	23
24	93–96	24
25	97–100	25
26	101–104	26
27	105–108	27
28	109–112	28
29	113–116	29
30	117–120	30