

Eighth Grade Math Overview

Math: Algebra 1/2

First Semester

Graphs
Decimals
Percentages
Measuring length, area, and volume
Algebraic equations
Rate word problems
Scientific notation

Second Semester

Ratios and proportions
Graphing inequalities
Negative coefficients
Estimating roots
Angles and triangles
Negative exponents
Permutations

Algebra $\frac{1}{2}$

An Incremental Development

Third Edition

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